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> restart;
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> with(linalg);
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[BlockDiagonal, GramSchmidt, JordanBlock, LUdecomp, QRdecomp, Wronskian, addcol, addrow, adj, adjoint, angle, augment, backsub, band, basis, bezout, blockmatrix, charmat, charpoly, cholesky, col, coldim, colspace, colspan, companion, concat, cond, copyinto, crossprod, curl, definite, delcols, delrows, det, diag, diverge, dotprod, eigenvals, eigenvalues, eigenvectors, eigenvects, entermatrix, equal, exponential, extend, ffgausselim, fibonacci, forwardsub, frobenius, gausselim, gaussjord, geneqns, genmatrix, grad, hadamard, hermite, hessian, hilbert, htranspose, ihermite, indexfunc, innerprod, intbasis, inverse, ismith, issimilar, iszero, jacobian, jordan, kernel, laplacian, leastsqrs, linsolve, matadd, matrix, minor, minpoly, mulcol, mulrow, multiply, norm, normalize, nullspace, orthog, permanent, pivot, potential, randmatrix, randvector, rank, ratform, row, rowdim, rowspace, rowspan, rref, scalarmul, singularvals, smith, stackmatrix, submatrix, subvector, sumbasis, swapcol, swaprow, sylvester, toeplitz, trace, transpose, vandermonde, vecpotent, vectdim, vector, wronskian]

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> M0 := Matrix([ [1, 0, 0, 0, 0, 0], [0, 1, 0, 0, 0, 0], [0, 0, 1, 0, 0, 0], [0, 0, 0, 1, 0, 0], [0, 0, 0, 0, 1, 0], [0, 0, 0, 0, 0, 1]]);
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$$M0 := \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \quad (2)$$

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> M1 := Matrix([ [0, 1, 1, 0, 0, 0], [s, s - 1, 0, 0, 1, 0], [s*(t2 + 1), 0, s - 1, t2 + 1, 1, 0], [0, 0, s*t2, (s - 1)*(t2 + 1), 0, 1], [0, s*(t2 + 1), s, 0, 2*(s - 1), t2 + 1], [0, 0, 0, s, s*t2, (s - 1)*(t2 + 2)]]);
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$$M1 := \begin{bmatrix} 0 & 1 & 1 & 0 & 0 & 0 \\ s & s - 1 & 0 & 0 & 1 & 0 \\ s(t2 + 1) & 0 & s - 1 & t2 + 1 & 1 & 0 \\ 0 & 0 & s t2 & (s - 1)(t2 + 1) & 0 & 1 \\ 0 & s(t2 + 1) & s & 0 & 2s - 2 & t2 + 1 \\ 0 & 0 & 0 & s & s t2 & (s - 1)(t2 + 2) \end{bmatrix} \quad (3)$$

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> eigvals1 := eigenvalues(M1);
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(4)

$$\text{eigvals}l := -t2 - 2, s - 2, 2s - 1, -t2 - 1 + s, s \cdot t2 + 2s, s \cdot t2 + s - 1 \quad (4)$$

$$> l1 := -t2 - 2;$$

$$l1 := -t2 - 2 \quad (5)$$

$$> l2 := -t2 - 1 + s;$$

$$l2 := -t2 - 1 + s \quad (6)$$

$$> l3 := s - 2;$$

$$l3 := s - 2 \quad (7)$$

$$> l4 := 2 \cdot s - 1;$$

$$l4 := 2s - 1 \quad (8)$$

$$> l5 := s \cdot t2 + s - 1;$$

$$l5 := s \cdot t2 + s - 1 \quad (9)$$

$$> l6 := s \cdot t2 + 2 \cdot s;$$

$$l6 := s \cdot t2 + 2s \quad (10)$$

$$> e1 := (s + 1)^2 \cdot (s \cdot t2 + 1);$$

$$e1 := (1 + s)^2 (s \cdot t2 + 1) \quad (11)$$

$$> e2 := 0;$$

$$e2 := 0 \quad (12)$$

$$> e3 := \text{expand}(\text{evalm}([0, 1, 1, 0, 0, 0].MI)[1] \cdot e1);$$

$$e3 := s^4 t2^2 + 2s^4 t2 + 2s^3 t2^2 + 5s^3 t2 + s^2 t2^2 + 2s^3 + 4s^2 t2 + 4s^2 + s t2 + 2s \quad (13)$$

$$> e4 := \text{expand}(\text{evalm}([0, 1, 1, 0, 0, 0].MI^2)[1] \cdot e1);$$

$$e4 := s^5 t2^2 + 2s^5 t2 + s^4 t2^2 + 3s^4 t2 - s^3 t2^2 + 2s^4 - s^3 t2 - s^2 t2^2 + 2s^3 - 3s^2 t2 - 2s^2 - s t2 - 2s \quad (14)$$

$$> e5 := \text{expand}(\text{evalm}([0, 1, 1, 0, 0, 0].MI^3)[1] \cdot e1);$$

$$e5 := s^5 t2^4 + s^6 t2^2 + 3s^5 t2^3 + 2s^4 t2^4 + 2s^6 t2 + 9s^5 t2^2 + 7s^4 t2^3 + s^3 t2^4 + 9s^5 t2 + 19s^4 t2^2 + 5s^3 t2^3 + 2s^5 + 21s^4 t2 + 15s^3 t2^2 + s^2 t2^3 + 8s^4 + 24s^3 t2 + 4s^2 t2^2 + 12s^3 + 11s^2 t2 + 8s^2 + s t2 + 2s \quad (15)$$

$$> e6 := \text{expand}(\text{evalm}([0, 1, 1, 0, 0, 0].MI^4)[1] \cdot e1);$$

$$e6 := s^6 t2^5 + 5s^6 t2^4 + s^5 t2^5 + s^7 t2^2 + 9s^6 t2^3 + 6s^5 t2^4 - s^4 t2^5 + 2s^7 t2 + 26s^6 t2^2 + 14s^5 t2^3 - 4s^4 t2^4 - s^3 t2^5 + 23s^6 t2 + 34s^5 t2^2 - 4s^4 t2^3 - 6s^3 t2^4 + 2s^6 + 46s^5 t2 - 16s^4 t2^2 - 14s^3 t2^3 - s^2 t2^4 + 22s^5 + 5s^4 t2 - 35s^3 t2^2 - 5s^2 t2^3 + 20s^4 - 47s^3 t2 - 10s^2 t2^2 - 20s^3 - 28s^2 t2 - 22s^2 - s t2 - 2s \quad (16)$$

> $V := \text{transpose}(\text{vandermonde}([l1, l2, l3, l4, l5, l6]));$

$$V := \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 \\ -t2 - 2 & -t2 - 1 + s & s - 2 & 2s - 1 & st2 + s - 1 & st2 + 2s \\ (-t2 - 2)^2 & (-t2 - 1 + s)^2 & (s - 2)^2 & (2s - 1)^2 & (st2 + s - 1)^2 & (st2 + 2s)^2 \\ (-t2 - 2)^3 & (-t2 - 1 + s)^3 & (s - 2)^3 & (2s - 1)^3 & (st2 + s - 1)^3 & (st2 + 2s)^3 \\ (-t2 - 2)^4 & (-t2 - 1 + s)^4 & (s - 2)^4 & (2s - 1)^4 & (st2 + s - 1)^4 & (st2 + 2s)^4 \\ (-t2 - 2)^5 & (-t2 - 1 + s)^5 & (s - 2)^5 & (2s - 1)^5 & (st2 + s - 1)^5 & (st2 + 2s)^5 \end{bmatrix} \quad (17)$$

> $W := \text{simplify}(\text{evalm}(\text{inverse}(V).\text{transpose}(\text{Matrix}([e1, e2, e3, e4, e5, e6]))));$

$$W := \begin{bmatrix} \frac{s^3 (st2 + 1)}{s + t2} \\ \frac{(st2 + 1) s^2}{s + t2} \\ \frac{(st2 + s + t2 + 1) s^2 t2}{s + t2} \\ \frac{(st2 + s + t2 + 1) s t2}{s + t2} \\ s \\ 1 \end{bmatrix} \quad (18)$$

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