A popular means of constructing elliptic curves with a given number of points proceeds by computing the Hilbert class polynomial of an imaginary quadratic field of some discriminant. Classically, this is done by approximating the values of the j-function in certain points of the upper half plane. In this talk, I will present a method that works over the p-adics instead of the complex numbers.